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! A one machine sequencing problem,
also known as the walking + biking problem.
Given one bicycle, and N persons,
and a distance they all must cover,
starting at the same time,
how much time should each person spend walking
and biking so they all cover the distance in minimum time;
!Ref: Chvatal, V.(1983), "On the Bicycle Problem,"
Discrete Applied Mathematics, North-Holland Publishing Company, 5 165-173
! Keywords: Bicycle, Biking, Chvatal, LINGO, One machine, Scheduling, Sequencing, Walking;
SETS:
  PERSON: W, B, X, U, Y, Z, Sorder;
ENDSETS
DATA:
! Case 1. From Chvatal. The lower bound (of 55)
  is tight for this data set.
! Input parameters;
! Distance to be covered;
!Case01; D = 100;
! Walking speeds;
!Case01; W = 1 2 1;
! Bicycling speeds;
!Case01; B = 6 8 6;

! Case 2. From Chvatal. The lower bound (of 10)
  is not tight for this data set. We cannot
  generate a feasible Walk->Bike->Walk schedule
  that achieves the LP bound;
!Input parameters;
! Distance to be covered;
!Case02 D = 90;
! Walking speeds;
!Case02 W = 13 13 3 3;
! Bicycling speeds;
!Case02 B = 27 27 18 18;

!Case 3;
! Input parameters;
! Distance to be covered;
!Case03 D = 100;
! Walking speeds;
!Case03 W = 1 2 3;
! Bicycling speeds;
!Case03 B = 6 8 9;

!Case 4;
! Input parameters;
! Distance to be covered;
!Case04 D = 100;
! Walking speeds;
!Case04 W = 1 1 1;
! Bicycling speeds;
!Case04 B = 3 3 3;

ENDDATA
! Variables for each person i:
  X( i) = total time walking forward,
  U( i) = total time walking backward,
  Y( i) = total time biking forward,
  Z( i) = total time biking backward,
;
SUBMODEL BikeWalk:
! This model contains constraints on an aggregate version
  of the bike & walk problem. Any complete detailed solution to the problem
  must satisfy at least these aggregate constraints,
  so the solution to this problem provides a lower bound;
MIN = T;

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@FOR( PERSON( i):
! Total travel time of person i <= T;
X( i) + U( i) + Y( i) + Z( i) <= T;
! Net distance of person i = D. Must get to destination;
W( i)* X( i) - W( i) * U( i) + B( i) * Y( i) - B( i) * Z( i) = D;
);

! Cannot use the bicycle more than total time T;
@SUM( PERSON( i): Y( i) + Z( i) <= T;

! In net the bicycle goes no further than D;
@SUM( PERSON( i): B( i) * Y( i) - B( i) * Z( i) <= D;
ENDSUBMODEL

CALC:
! Solve the aggregate, relaxed problem;
! @GEN( BikeWalk); ! Generate the scalar version of model;
@SOLVE( BikeWalk);
@WRITE( ' Total time= ', T, @NEWLINE(1));
@WRITE( ' Distances', @NEWLINE(1));
@WRITE(' Person Walk+ Walk- Bike+ Bike-', @NEWLINE( 1));
@FOR( PERSON( i):
@WRITE(' ', i, ' ', @FORMAT( W( i)* X( i),'9.3f'), ' ', @FORMAT( W( i) * U(
i),'9.3f'),
' ', @FORMAT( B( i) * Y( i),'9.3f'), ' ', @FORMAT( B( i) * Z( i), '9.3f'),
@NEWLINE(1));
);

@WRITE( @NEWLINE( 1),' Times', @NEWLINE(1));
@WRITE(' Person Walk+ Walk- Bike+ Bike-', @NEWLINE( 1));
@FOR( PERSON( i):
@WRITE(' ', i, ' ', @FORMAT( X( i),'9.3f'), ' ', @FORMAT( U( i),'9.3f'),
' ', @FORMAT( Y( i),'9.3f'), ' ', @FORMAT( Z( i), '9.3f'), @NEWLINE(1));
);

! Do postprocessing to (hopefully) get a feasible detailed solution
that achieves the lower bound, and is thus optimal;
! We restrict ourselves to Walk->Bike->Walk schedules, i.e., each person
first walks to the bike, then bikes for awhile(perhaps backwards), and
then walks the remaining distance.
The detailed schedule is feasible if the person i-1 finishes its use of the bike
before the person i, who needs the bike, arrives at the bike position;
@WRITE( @NEWLINE( 1), ' The detailed schedule:', @NEWLINE( 1));
! Choose a sort order. Put fast cyclists first;
Sorder = @SORT( - B);
! But if fast cyclist goes backwards, do not put first;
@IFC( Z( sorder( 1) #GT# 0:
temp = Sorder( 2); ! Swap with #2;
Sorder( 2) = Sorder( 1);
Sorder( 1) = temp;
);
BikeAt = 0; ! Initial position of Bike;
BFtimePrv = 0; ! Time available of Bike;
! Loop over the persons, computing their
Walk, Bike, Walk positions and times;
@FOR( PERSON( i):
si = Sorder( i); ! Use sort order;
! Arrive at Bike time after first walk;
ATime = BikeAt/ W( si);
! Calculate bike ride incremental distance;
Bdist = B( si) * Y( si) - B( si) * Z( si);
! Calculate bike ride incremental time;
Btime = Y( si) + Z( si) ;
! Ending position of bike for person i;
Bend = BikeAt + Bdist;
! Ending time of bike for person i;
BFtime = Atime + Btime;
@WRITE( ' Person ', PERSON( si),

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'12.4f'),
'12.4f'),
'12.4f'),
' walk to ', @FORMAT( BikeAt,'12.4f'),' Time= ', @FORMAT( Atime,
' Bike to ', @FORMAT( Bend,'12.4f'), ' Time= ', @FORMAT( BFtime,
' Walk to ', @FORMAT( D,'12.4f'), , @NEWLINE( 1));
! Check if feasible, i.e., person i-1 finishes bike use before i needs it;
@IFC( BFtime #LT# BFtimePrv:
@WRITE( 'Schedule not feasible', @NEWLINE( 1));
);
BFtimePrv = BFtime; ! Get ready for next i;
! And we leave the bike for next person at;
BikeAt = Bend;
);
ENDCALC

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