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! General Equilibrium Model of an economy, (GenEqIbx);
! Data based on Kehoe, Math Prog, Study 23(1985), page 253;
! Find clearing prices for commodities/goods and
equilibrium production levels for processes in
an economy.
```

```
    This model has multiple equilibria. Three of them are:
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	PRICE(1)	PRICE(2)	PRICE(3)	PRICE(4)	LEVEL(1)	LEVEL(2)
1)	1	1	1	1	52	69
2)	0.637688	1	0.154606	2.207706	42.70128	81.19803
3)	1.100547	1	1.234609	0.664845	53.18013	65.14815

```
Ref: Kehoe, T. J.(1985), "A numerical investigation of multiplicity of equilibria,"
Mathematical Programming Study 23, pp. 240-258. ;
```

```
! Keywords: Complementarity constraints, Equilibrium, General equilibrium,
Kehoe, LINGO, Multiple solutions;
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```
SETS:
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```
GOOD: PRICE, H;
SECTOR;
GXS( GOOD, SECTOR): ALPHA, W;
PROCESS: LEVEL, RC;
GXP( GOOD, PROCESS): MAKE;
```

```
ENDSETS
```

```
DATA:
```

```
! There are 4 goods, 4 sectors. In general need not be same number;
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```
GOOD = 1..4;
```

```
SECTOR = 1..4;
```

```
! Demand curve parameter for each good i & sector j;
```

```
ALPHA =
.5200 .8600 .5000 .0600
.4000 .1 .2 .25
.04 .02 .2975 .0025
.04 .02 .0025 .6875;
```

```
! Initial wealth of good i by for sector j;
```

```
W =
50 0 0 0
0 50 0 0
0 0 400 0
0 0 0 400;
```

```
PROCESS= 1 2; ! There are two processes to make goods;
```

```
!Amount produced of good i per unit of process j;
```

```
MAKE =
6 -1
-1 3
-4 -1
-1 -1;
```

```
! Weights for price normalization constraint;
```

```
H = .25 .25 .25 .25;
```

```
ENDDATA
```

```
!-----;
```

```
! Variables:
```

```
LEVEL(p) = level or amount at which we operate
           process p.
RC(p) = reduced cost of process p,
        = cost of inputs to process p - revenues from outputs
          of process p, per unit.
PRICE(g) = equilibrium price for good g;
```

```
! Constraints;
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```
! For each good G, we must have supply = demand, i.e.,
initial amount + production = sum over sectors, S,
of amount demanded of G at given prices;
```

```
@FOR( GOOD( G) :
```

```
  @SUM( SECTOR( M): W( G, M))
+ @SUM( PROCESS( P): MAKE( G, P) * LEVEL( P))
= @SUM( SECTOR( S) :
  ALPHA( G, S) *
  @SUM( GOOD( I): PRICE( I) * W( I, S))/ PRICE( G));
);
```

```

! Each process at best breaks even. RC is constrained >= 0;
@FOR( PROCESS( P):
    RC( P) = @SUM( GOOD( G): - MAKE( G, P) * PRICE( G));
! Complementarity constraints.
    If process p has a positive opportunity cost (RC > 0),
    then do not use it (LEVEL = 0).
    Also, if use it ( LEVEL > 0),
    then must not have a positive opportunity cost (RC = 0);
    RC( P)*LEVEL( P) = 0;
    );

! Price normalization constraint. Choose prices scale to 1.
    Without a scaling constraint there can be an infinity of solutions;
    @SUM( GOOD( G): H( G) * PRICE( G)) = 1;

! You can arbitrarily limit to a particular solution by
    bounding the prices.
    Be sure to turn on the global solver by clicking:
    LINGO -> Options -> Global;
! @BND( 0, PRICE( 1), .65);
! @BND( 0.65, PRICE( 1), 1.05);
@BND( 1.05, PRICE( 1), 9999);

```